Performing critical path analysis

The tips and tricks below are taken from Project Mentor, the smart way to learn Microsoft Project. For further information, please go to:

www.projectlearning.net/project_mentor.htm

More useful tips and tricks can be found on the Project Learning blog:

www.projectknowledge.net

Related document(s):

Displaying a Critical Path  www.projectlearning.net/pdf/C2.1.pdf

Document author: Andy Jessop
Produced by: Project Learning International Limited
www.projectlearning.net
Performing critical path analysis

Introduction

A basic understanding of how a project's schedule is calculated can provide a much clearer understanding of what should happen when. At the heart of Microsoft Project is an algorithm that uses critical path analysis (CPA) to calculate a project's schedule. Most Microsoft Project users are either unaware of the CPA algorithm at all, or they are unsure as to how it performs its calculations.

These tips and tricks follow the CPA process step-by-step and provide a clear insight into how project schedules are calculated by Microsoft Project.

Background

As the tasks within a project have links between them, they cannot all happen at the same time. A technique entitled critical path analysis (CPA) can be used to determine what can happen when. It calculates how quickly and how slowly the tasks can be performed, taking into account the sequence of tasks and the interrelationships between them. Project reports such as Gantt charts are created as a result of critical path analysis.
What critical path analysis calculates

Critical path analysis (CPA) is a mathematical procedure that calculates a project's schedule. Taking each task in turn it firstly calculates how quickly the task can be accomplished - its early start and early finish dates. Once all these dates have been calculated, the project finish date can also be determined. With this finish date known, CPA can then calculate how slowly each task can be accomplished (late start and late finish dates). Once all this information is known for each task, CPA will also calculate the slack (or float) that the task possesses.

- Take the network of tasks and list the task’s name and duration:

- Consider that the following values need to be calculated:

\[
\begin{array}{cccc}
\text{ES} & \text{EF} & \text{LS} & \text{TS} & \text{LF} \\
\text{Task name} & & & & \\
\end{array}
\]

ES = Early Start
EF = Early Finish
LS = Late Start
LF = Late Finish
TS = Total Slack
Performing critical path analysis

Calculating early dates for tasks

Early start and early finish dates for tasks are calculated by a process known as a forward pass. This proceeds through the project's network from the earliest occurring tasks (positioned to the left side of the diagram) to the latest occurring tasks (positioned to the right side of the diagram):

<table>
<thead>
<tr>
<th>ES</th>
<th>1 day</th>
<th>EF</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Task name</td>
</tr>
</tbody>
</table>

a. Enter an ES value of 0 for any task that has no predecessor (as it can commence straight away).

b. For each of the tasks with ES=0 values, their EF value will be calculated from the ES value PLUS the task's duration (for example; 'Design Structure' will have ES=0 and EF=5 (day number 5 of the project)).

c. As 'Write body text' and 'Create exercises' have a common predecessor, the ES value for BOTH of them will be the same as the EF value for their common predecessor; day 5.

d. The EF for 'Write body text' is calculated by ADDING the duration value (in this case 15 days) to the tasks ES value (day 5), thus finishing on day 20.

e. The EF for 'Create exercises' is calculated as operation four, with EF = ES+Duration (5+10 = day 15).

f. 'Set page layouts' can commence as soon as its predecessor is complete; day 20.

g. 'Test exercises' can commence once its predecessor is complete; day 15.

h. EF values for 'Set page layouts' & 'Test exercises' can be calculated as EF = ES+Duration (days 25 and 20 respectively).

i. As 'Create contents and index' has multiple predecessors, it can only commence when ALL of them are complete. Its ES value is therefore day 25 (the EF of its LATEST predecessor).

j. The EF for 'Create contents and index' is simply ES+Duration - day 30. The project finish date is therefore day 30.
Performing critical path analysis

The calculated diagram would look like this:

```
<table>
<thead>
<tr>
<th>Task</th>
<th>Duration</th>
<th>Start</th>
</tr>
</thead>
<tbody>
<tr>
<td>Design structure</td>
<td>5 days</td>
<td>0</td>
</tr>
<tr>
<td>Write body text</td>
<td>15 days</td>
<td>5</td>
</tr>
<tr>
<td>Set page layouts</td>
<td>20 days</td>
<td>20</td>
</tr>
<tr>
<td>Create contents &amp; index</td>
<td>25 days</td>
<td>25</td>
</tr>
<tr>
<td>Create exercises</td>
<td>10 days</td>
<td>5</td>
</tr>
<tr>
<td>Test exercises</td>
<td>5 days</td>
<td>15</td>
</tr>
</tbody>
</table>
```

Hints

- Don't enter an ES value for a task until the EF values for ALL of its predecessors have been calculated.
Calculating late dates for tasks

Working through the network diagram from right to left, the backward pass calculates late start and late finish dates for each task:

<table>
<thead>
<tr>
<th>1 day</th>
<th>Task name</th>
<th>LS</th>
<th>LF</th>
</tr>
</thead>
</table>

a. For all tasks without successors (in this case 'Create contents and index') the LF date will be the same as the EF date; day 30.

b. The LS for 'Create contents and index' is calculated by SUBTRACTING the task's duration from its EF value (LS = LF-Duration); that is 30-5 = day 25.

c. The LF values for ALL the immediate predecessors of 'Create contents and index' will be day 25 (the same as the 'Create contents and index' LS value).

d. 'Set page layout' will have a LS of day 20 (LF-Duration); 25-5

e. 'Test exercises' will also have a LS of day 20 (LF-Duration); 25-5

f. The LF of 'Write body text' is equivalent to the LS of its immediate successor ('Set page layouts', day 20).

g. The LF of 'Create exercises' is equivalent to the LS of its immediate successor ('Test exercises', day 20).

h. The LS for 'Write body text' and 'Create exercises' is calculated as LS = LF-Duration (days 5 and 10 respectively).

i. As 'Design structure' must be complete before any of its successors can commence, its LF value will be equivalent to the EARLIEST LS value for its successors, in this case day 5.

j. LS for 'Design structure' is simply its LF-Duration; day 0.
Performing critical path analysis

The calculated diagram would look like this:

<table>
<thead>
<tr>
<th>Hints</th>
</tr>
</thead>
<tbody>
<tr>
<td>• Don’t enter an LF value for a task until the LS values for ALL of its successors have been calculated.</td>
</tr>
</tbody>
</table>
Performing critical path analysis

Finding tasks with spare time

As the backward pass has determined how slowly work can be accomplished, there is often a difference between late and early values. Tasks possessing a difference between early and late dates are said to possess slack (or float). These tasks are known as non-critical tasks.

| 1 day |
| Task name |
| TS |

- To calculate slack values for each task, use the formula: \( TS = LF - ES - \text{Duration} \)

The calculated diagram would look like this:

Hints

- Exercise caution in telling people in your workgroup about slack – as they may be tempted to use it without you knowing.
Performing critical path analysis

Highlighting critical tasks

Some tasks possess no slack. They are known as critical tasks. Any delay to them (or the path that they are on) will in turn delay the project’s end date. Critical tasks in a sequence are referred to as the critical path. Conventions usually state that critical paths are usually highlighted in red, and non-critical paths are shown in blue:

**Hints**
- Tasks that are non-critical may still require careful management.